

# Logic I: Lecture 13

s.butterfill@warwick.ac.uk

Readings refer to sections of the course textbook, *Language, Proof and Logic*.

## 1. There Is a Store for Everything

Reading: §11.2, §11.3

There is a store for everything:

$$\exists y \forall x \text{ StoreFor}(y,x)$$

$$\forall y \exists x \text{ StoreFor}(x,y)$$

Other sentences to translate:

Wikipedia has an article about everything

Everyone hurts someone they love

Someone hurts everyone she loves

## 2. How Big Is a Truth-Table?

How many truth-functions can be constructed using 2 sentence letters?

P	Q	P % Q
T	T	?
T	F	?
F	T	?
F	F	?

Each of these can be T or F

## 3. Truth-functional completeness

Reading: §7.4

'A set of truth-functores is said to be *expressively adequate* (or sometimes *functionally complete*) iff, for every truth-function whatever, there is a formula containing only those truth-functores which express that truth-function, i.e. which has as its truth-table the truth-table specifying that function.' (Bostock, *Intermediate Logic* p. 45)

Illustration of the proof that  $\{\neg, \wedge, \vee\}$  is truth-functionally complete:

P	Q	$P \rightarrow Q$	
T	T	T	$[P \wedge Q] \vee$
T	F	F	
F	T	T	$[\neg P \wedge Q] \vee$
F	F	T	$[\neg P \wedge \neg Q]$

$$[P \wedge Q] \vee [\neg P \wedge Q] \vee [\neg P \wedge \neg Q]$$

Exercise assuming  $\{\neg, \vee, \wedge\}$  is truth-functionally complete, show that  $\{\neg, \vee\}$  is.